## Toughness treshold for the existence of 2-walks in $K_4$ -minor free graphs

## Jakub Teska<sup>1</sup>.

joint work with Zdeněk Dvořák<br/>2 and Daniel Král'²

## Abstract

A 2-walk is a closed spanning trail which uses every vertex at most twice. The toughness of a non-complete graph is  $t(G) = \min(\frac{|S|}{c(G-S)})$ , where the minimum is taken over all nonempty vertex sets S, for which  $c(G-S) \ge 2$  and c(G-S) denotes the number of components of the graph G-S. We show that every  $K_4$ -minor free graph with toughness  $t(G) > \frac{4}{7}$  has a 2-walk. We also give an example of a  $\frac{4}{7}$ -tough  $K_4$ -minor free graph with no 2-walk.

## References

- D. Bauer, H. J. Broersma, E. Schmeichel. More progress on tough graphs-The Y2K-report. *Electronic Notes in Discrete Math* 11 (2000).
- [2] T. Bőhme, J. Harant, M. Tk. More than one tough chordal planar graphs are hamiltonian. J. Graph Theory 32 (1999), 405-410.
- [3] M. N. Ellingham, X. Zha. Toughness, trees, and walks. J. Graph Theory 33 (2000), 125-137.
- [4] G. Chen, M. S. Jacobson, A. E. Kzdy, J. Lehel. Tough enough chordal graphs are hamiltonian. *Networks* 31 (1997), 29-38.
- [5] V. Chvtal. Tough graphs and hamiltonian circuits. Discrete Math. 5 (1973), 215-228.

 $<sup>^1</sup>$ School of ITMS, University of Ballarat, VIC 3353, Australia, Department of Mathematics, University of West Bohemia, Universitní 8, 306 14 Plzeň, Czech Republicteska@kma.zcu.cz

<sup>&</sup>lt;sup>2</sup>Institute for Theoretical Computer Science (ITI), Faculty of Mathematics and Physics, Charles University, Malostranské Náměstí 25, 118 00 Prague 1, Czech Republic {*rakdver,kral*}@*kam.mff.cuni.cz.* Institute for Theoretical Computer Science is supported as project 1M0021620808 by Czech Ministry of Education.